

PROBLEM SET 1  
ECE 311 Autumn Quarter 2008

Assigned: September 24th

Due: October 3rd in class

Instructor: Joel Johnson

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Problem 1

If “appreciable” means “larger than 10%,” find the highest frequency for which the following devices can be treated using standard circuit theory.

- (a) a CMOS device with horizontal dimensions of 0.22 microns by 0.22 microns
- (b) a 15 cm long wire used in the ECE circuits lab
- (c) a power line with length 400 km
- (d) a 1.2 m long USB cable

Problem 2

Given  $a = 8 + 7j$  and  $b = 3 - 9j$ , find

- (a) the polar form for  $a$ .
- (b) the rectangular form for  $a + b$ .
- (c) the rectangular form of  $a/b$ .
- (d) the polar form of  $ab$ .
- (e) write  $v(t) = 4 \sin(\omega t + 5^\circ)$  V in phasor form.
- (f) write  $v(t) = 2 \cos(\omega t) - 4 \sin(\omega t)$  V in phasor form.

Problem 3

A transmission line operated at a frequency of 3 GHz has  $\gamma = 0.2 + j5\pi$  (per meter). It is also known that the line’s characteristic impedance is  $Z_0 = 100 + j1$  Ohms.

- (a) Is this a lossless line?
- (b) Find the attenuation constant  $\alpha$  and the phase constant  $\beta$ . Include units.
- (c) Find the parameters  $R'$ ,  $G'$ ,  $L'$ , and  $C'$  of this line. Include units.

Problem 4

The voltage on a transmission line is known to be

$$\tilde{V}(z) = 0.4e^{-j5\pi z} + 0.4e^{j5\pi z} \text{ Volts}$$

with  $z$  in units of meters.

- (a) Find  $V_0^+$  and  $V_0^-$ .
- (b) Find  $\alpha$ ,  $\beta$ , and  $\gamma$ .
- (c) If the line has characteristic impedance  $Z_0 = 100$  Ohms, find  $\tilde{I}(z)$ .
- (d) Find  $v(z, t)$ . Try to simplify as much as possible.
- (e) Sketch  $v(z, 0)$ ,  $v\left(z, t = \frac{\pi}{2\omega}\right)$ , and  $v\left(z, t = \frac{3\pi}{2\omega}\right)$  (i.e. voltages versus space at the specified times) for  $z=0$  to 0.8 m. Interpret your results. Do these plots look like the voltage along a wire in circuit theory?